YFAR 10 - USING NUMBER

144

@whisto maths

Indices & Roots

What do I need to be able to do?

By the end of this unit you should be able to:

- Identify square and cube numbers
- Calculate higher powers and roots
- Understand powers of 10 and standard
- Know the addition and subtraction rule for
- Understand power zero and negative indices
- Calculate with numbers in standard form

Keywords

Standard (index) Form: A system of writing very big or very small numbers

Commutative: an operation is commutative if changing the order does not change the result.

Base: The number that gets multiplied by a power

Power: The exponent — or the number that tells you how many times to use the number in multiplication. Exponent: The power — or the number that tells you how many times to use the number in multiplication.

Indices: The power or the exponent.

Negative: a value below zero...

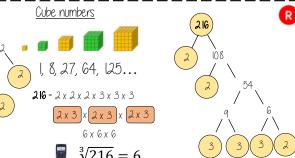
Coefficient: The number used to multiply a variable

Square and cube numbers Square numbers

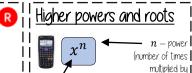




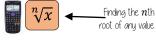












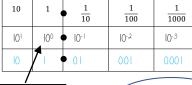
itself) |

Other mental strategies for square roots $\sqrt{810000} = \sqrt{81} \times \sqrt{10000}$

Standard form Ony integer Onu number

less than 10





 $= 9 \times 100$ = 900

Example

3.2 x 10 4

Non-example 0.8 x 10 4

= 3.2 x 10 x 10 x 10 x 10

= 32000

5.3 x 10⁰⁷

Numbers in standard form with negative powers will be less than I

Ony value to the power O always = 1

 $3.2 \times 10^{-4} = 3.2 \times \frac{1}{10} \times \frac{1}{10} \times \frac{1}{10} \times \frac{1}{10} = 000032$

Oddition/Subtraction Laws

 $a^m \times a^n = a^{m+n}$

 $a^m \div a^n = a^{m-n}$

Zero and negative indices

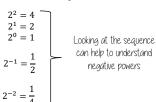
$$x^0 = 1$$

Ony number divided by itself = 1

$$\frac{a^6}{a^6} = a^6 \div a^6$$

$$= a^{6-6} = a^0 = 1$$

Negative indices do not indicate negative solutions



Powers of powers

$$(x^a)^b = x^{ab}$$

$$(2^3)^4 = 2^3 \times 2^3 \times 2^3 \times 2^3$$

The same base and power is repeated Use the addition

$$(2^3)^4 = 2^{12} - a \times b = 3 \times 4 = 12$$

NOTICE the difference

$$(2x^3)^4 = 2x^3 \times 2x^3 \times 2x^3 \times 2x^3$$

The addition law applies ONLY to the powers. The integers still need to be multiplied

$$(2x^3)^4 = 16x^{12}$$

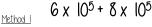
Standard form calculations

Oddition and Subtraction

Negative powers do not

indicate negative solutions

Tip: Convert into ordinary numbers first and back to standard from at



= 600000 + 800000

Multiplication and division

= 1400000

 $= 1.4 \times 10^{5}$

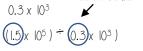
 $= (6 + 8) \times 10^{5}$ 14 x 10⁵

This is not the 1.4 x 101 x 105 final answer

= 1.4 x 10⁵

Method 2

Division questions can look like this



 $1.5 \div 0.3$ x $10^5 \div 10^3$

 $=5 \times 10^{2}$

For multiplication and division you can look at the values for A and the powers of 10 as two separate calculations