## YFAR 10 - SIMILARITY...

## @whisto maths

# Trigonometry

#### What do I need to be able to do?

By the end of this unit you should be able to:

- Work fluently with hypotenuse, opposite and adjacent sides
- Use the tan, sine and cosine ratio to find missing side lengths
- Use the tan, sine and cosine ratio to find missing anales
- Calculate sides using Pythagoras'

#### Keywords

When the angle is the same

**Enlarge**: to make a shape bigger (or smaller) by a given multiplier (scale factor)

Scale Factor: the multiplier of enlargement

Constant: a value that remains the same

Cosine ratio: the ratio of the length of the adjacent side to that of the hypotenuse. The sine of the complement

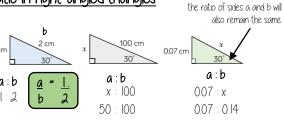
Sine ratio: the ratio of the length of the opposite side to that of the hypotenuse.

**Tangent ratio**: the ratio of the length of the opposite side to that of the adjacent side.

Inverse: function that has the opposite effect.

Hypoteruse: longest side of a right-angled triangle. It is the side opposite the right-angle

### Ratio in right-angled triangles

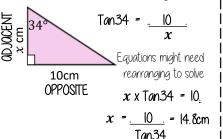


Hupotenuse, adjacent and opposite ONLY right-angled triangles are labelled in **ADJACENT** OPPOSITE Next to the angle in question Often labelled last Olways opposite an acute angle Useful to label second Position depend upon the angle Olways the longest side in use for the question HYPOTENUSE always opposite the right angle

#### Tangent ratio: side lengths

 $Tan\theta$  = opposite side adjacent side

Substitute the values into the tangent formula !



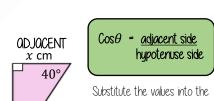
hupotenuse side NOTE The Sin(x) ratio is 12 cm HYPOTENUSE the same as the Cos(90-x) ratio

 $Sin\theta$  = opposite side

Sin and Cos ratio: side lengths

OPPOSITE

x cm



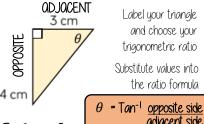
ratio formula 12 cm Equations might need HYPOTENUSE rearranging to solve

Useful to label this first

## Sin, Cos, Tan: Ongles

 $\theta = 36.9^{\circ}$ 

#### Inverse trigonometric functions

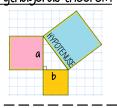


adjacent side  $Tan\theta =$  $\theta$  = Sin<sup>-1</sup> opposite side

hypotenuse side  $\theta$  = Tan<sup>-1</sup> 3 = Cos-1 adiacent side

hypotenuse side

## Pythagoras theorem 🔞



Hupotenuse<sup>2</sup> =  $a^2 + b^2$ 

This is commutative — the square of the hypotenuse is equal to the sum of the squares of the two shorter

Because trig ratios remain the same for similar

#### Places to look out for Pythagoras Perpendicular heights in isosceles

- trianales Diagonals on right angled shapes
- Distance between coordinates

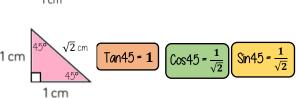
#### Ony length made from a right angles

#### Keu anales

√3 cm

This side could be calculated using Pythagoras

shapes you can generalise from the following statements.  $\cos 30 = \frac{\sqrt{3}}{3}$ Sin30 =  $\Gamma an 30 = \frac{1}{\sqrt{3}}$ Sin60 =  $\frac{\sqrt{3}}{1}$  $\cos 60 = \frac{1}{2}$  $\lceil an60 = \sqrt{3}$ 1 cm



## Key anales 0° and 90°

Tan0 = 0

This value cannot be defined — it is impossible as you cannot have two 90° angles in a triangle

Sin0 = 0Sin90 = 1

Cos0 = 1Cos90 = 0