

BLOCK: SIMILARITY

Congruence, similarity & enlargement

Trigonometry

## YEAR 10 - SIMILARITY

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## Congruence, similarity & enlargement

#### What do I need to be able to do?

#### By the end of this unit you should be able

- Enlarge by a positive scale factor
- Enlarge by a fractional scale factor
- Identify similar shapes
- Work out missing sides and angles in similar shapes
- Use parallel lines to find missing angles
- Understand similarity and congruence

#### Keywords

Enlarge: to make a shape bigger (or smaller) by a given multiplier (scale factor)

Scale Factor: the multiplier of enlargement

**Centre of enlargement**: the point the shape is enlarged from

Similar: when one shape can become another with a reflection, rotation, enlargement or translation.

Congruent: the same size and shape

Corresponding: items that appear in the same place in two similar situations

Parallel: straight lines that never meet (equal gradients)

#### Positive scale factors 🔞

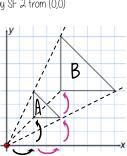


Enlargement from a point

Enlarge shape A by SF 2 from (0,0)

The shape is enlarged by 2

The distance from the point enlarges by 2



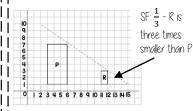
change with scale

#### Fractional scale factors



I Fractions less than I make a shape SMOLLER

R is an enlargement of P by a scale factor  $\frac{1}{2}$  from centre of enlargement (15,1)



#### Identify similar shapes



Ongles in similar shapes do not

e.g. if a triangle gets bigger the anales can not ao above 180º





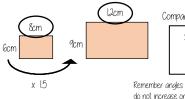
Scale Factor: Both sides on the bigger

Co-interior angles

8 12 2:3

Both sets of sides are in the same ratio

#### Information in similar shapes



Compare the equivalent side on both shapes

Scale Factor is the multiplicative relationship between the two lengths

Shape OBCD and EFGH are similar

Notation helps us corresponding sides

#### Ongles in parallel lines 🔞 Olternate angles

Corresponding anales

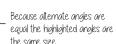
are the same size

Because corresponding angles

are equal the highlighted angles

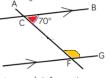


Compare



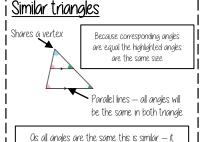
Because co-interior angles have a sum of 180° the highlighted angle is 110°

shape are 15 times bigger



Os angles on a line add up to 180° co-interior angles can also be calculated from applying alternate/corresponding rules

#### **QB** and EF are corresponding



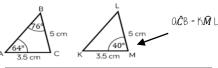
only one pair of sides are needed to show equality

Oll the angles in both triangles are the same and so Vertically opposite angles

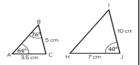
#### Congruence and Similarity

10.5cm

Congruent shapes are identical — all corresponding sides and angles are the same size



Because all the angles are the same and OC=KM BC=LM triangles OBC and KLM are congruent



Because all angles are the same, but all sides are enlarged by 2 OBC and HLJ are

#### Conditions for congruent triangles

Triangles are congruent if they satisfy any of the following conditions

#### Side-side-side

Oll three sides on the triangle are the same size

#### Ongle-side-angle

Two angles and the side connecting them are equal in two

#### Side-angle-side

Two sides and the angle in-between them are equal in two triangles (it will also mean the third side is the same size on both shapes)

#### Right angle-hypotenuse-side

The triangles both have a right angle, the hypotenuse and one side are the same

## YEAR 10 - SIMILARITY...

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## Trigonometry

#### What do I need to be able to do?

By the end of this unit you should be able to:

- Work fluently with hypotenuse, opposite and adjacent sides
- Use the tan, sine and cosine ratio to find missing side lengths
- Use the tan, sine and cosine ratio to find missing anales
- Calculate sides using Pythagoras'

#### Keywords

When the angle is the same

**Enlarge**: to make a shape bigger (or smaller) by a given multiplier (scale factor)

Scale Factor: the multiplier of enlargement

Constant: a value that remains the same

Cosine ratio: the ratio of the length of the adjacent side to that of the hypotenuse. The sine of the complement

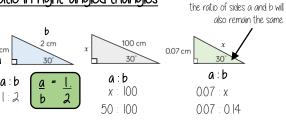
Sine ratio: the ratio of the length of the opposite side to that of the hypotenuse.

**Tangent ratio**: the ratio of the length of the opposite side to that of the adjacent side.

Inverse: function that has the opposite effect.

Hypoteruse: longest side of a right-angled triangle. It is the side opposite the right-angle

#### Ratio in right-angled triangles

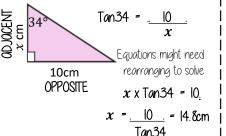


Hupotenuse, adjacent and opposite ONLY right-angled triangles are labelled in **ADJACENT** OPPOSITE Next to the angle in question Often labelled last Olways opposite an acute angle Useful to label second Position depend upon the angle Olways the longest side in use for the question HYPOTENUSE always opposite the right angle

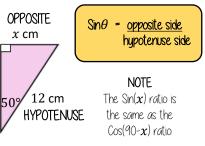
#### Tangent ratio: side lengths

 $Tan\theta$  = opposite side adjacent side

Substitute the values into the tangent formula !



#### Sin and Cos ratio: side lengths

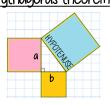


 $Cos\theta$  = adjacent side **ADJACENT** hypotenuse side x cm40° Substitute the values into the

> ratio formula 12 cm Equations might need HYPOTENUSE rearranging to solve

Useful to label this first

#### Pythagoras theorem 🔞



Hupotenuse<sup>2</sup> =  $a^2 + b^2$ 

Sin45 =

This is commutative — the square of the hypotenuse is equal to the sum of the squares of the two shorter

Cos45 =

#### Places to look out for Pythagoras Perpendicular heights in isosceles

- trianales Diagonals on right angled shapes
- Distance between coordinates
  - Ony length made from a right angles

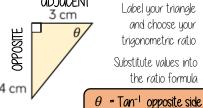
Key anales 0° and 90°

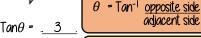
#### Sin, Cos, Tan: Ongles

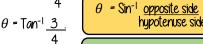
**ADJACENT** 

 $\theta = 36.9^{\circ}$ 

#### Inverse trigonometric functions







hypotenuse side = Cos-1 adiacent side

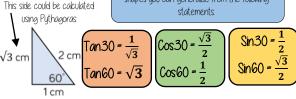
hypotenuse side

#### Keu anales

1 cm

1 cm

Because trig ratios remain the same for similar shapes you can generalise from the following This side could be calculated statements. using Pythagoras

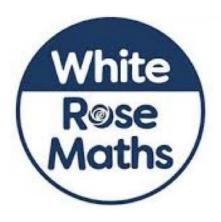


Tan45 = 1

This value cannot be defined — it is impossible as you cannot have two 90° angles in a triangle Sin0 = 0Sin90 = 1

Tan0 = 0

Cos0 = 1Cos90 = 0



BLOCK: DEVELOPING ALGEBRA

Representing solutions of equations and inequalities

Simultaneous equations

## YEAR 10 - DEVELOPING ALGEBRA...

## Representing solutions of equations and

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inequalities

#### What do I need to be able to do?

By the end of this unit you should be able to:

- Form and solve equations and inequalities
- Represent and interpret solutions on a number line as inequalities
- Draw straight line graphs and find solutions to equations
- Form and solve equations and inequalities with unknowns on both sides

#### <u>Keywords</u>

Solution: a value we can put in place of a variable that makes the equation true

Variable: a symbol for a number we don't know yet.

**Equation**: an equation says that two things are equal — it will have an equals sign =

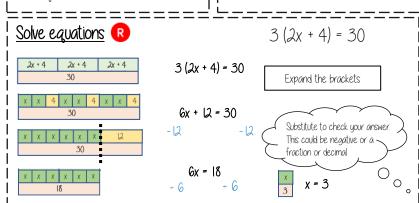
Expression: numbers, symbols and operators grouped together to show the value of something

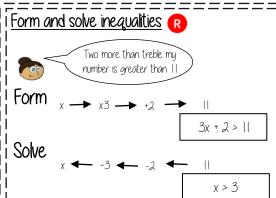
**Identity**: On equation where both sides have variables that cause the same answer includes  $\equiv$ 

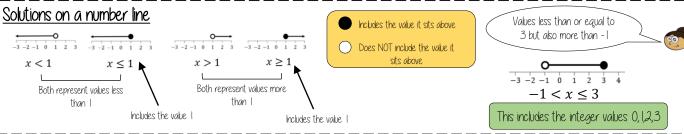
Linear: an equation or function that is the equation of a straight line

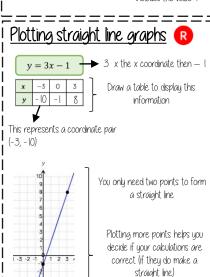
Intersection: the point that two lines meet

Inequality: an inequality compares two values showing if one is greater than, less than or equal to another.

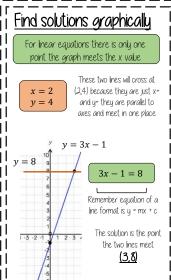


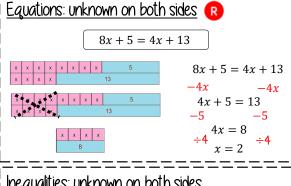


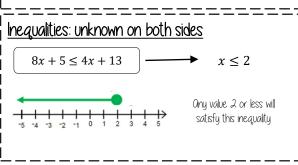




Remember to join the points to make a line







## YEAR 10 - DEVELOPING ALGEBRA...

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## Simultaneous Equations

#### What do I need to be able to do?

By the end of this unit you should be able to:

- Determine whether (x,y) is a solution
- Solve by substituting a known variable
- Solve by substituting an expression
- Solve araphically
- Solve by subtracting/ adding equations
- Solve by adjusting equations
- Form and solve linear simultaneous equations

#### Keywords

Solution: a value we can put in place of a variable that makes the equation true

Variable: a symbol for a number we don't know yet.

**Equation**: an equation says that two things are equal - it will have an equals sign =

Substitute: replace a variable with a numerical value

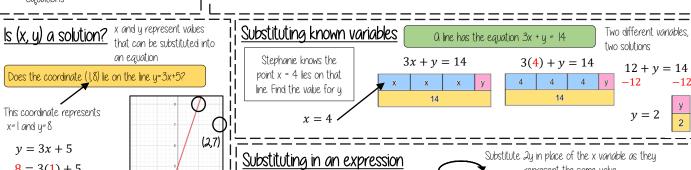
LCM: lowest common multiple (the first time the times table of two or more numbers match)

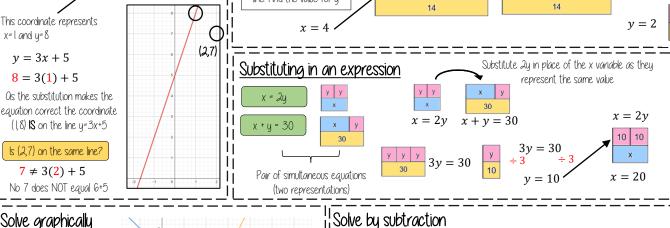
Eliminate: to remove

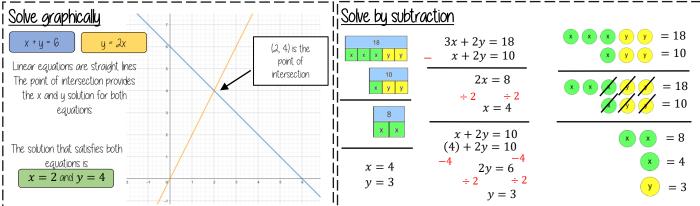
Expression: a maths sentence with a minimum of two numbers and at least one math operation (no equals sign)

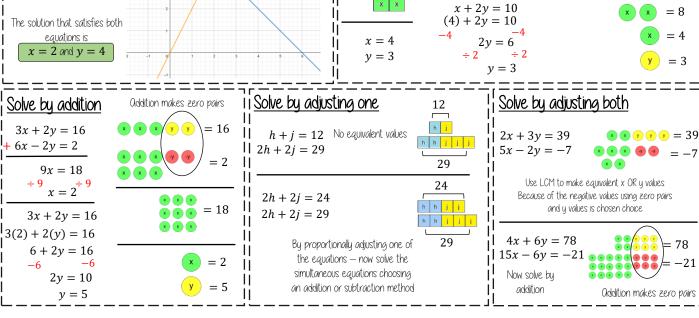
**Coordinate**: a set of values that show an exact position.

Intersection: the point two lines cross or meet











BLOCK: GEOMETRY

Ongles and bearings
Working with circles
Vectors

## YEAR 10 - GEOMETRY...

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## Ongles and bearings

#### What do I need to be able to do?

#### By the end of this unit you should be able to:

- Understand and represent bearings
- Measure and read bearings
- Make scale drawings using bearings
- Calculate bearings using angle rules
- Solve bearings problems using Puthagoras and trigonometry

#### Keywords

Cardinal directions: the directions of North, South, East, West

Ongle: the amount of turn between two lines around their common point

Bearing: the angle in degrees measured clockwise from North.

Perpendicular: where two lines meet at 90°

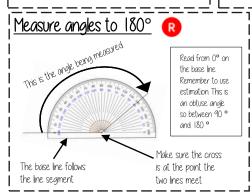
Parallel: straight lines always the same distance apart and never touch. They have the same gradient.

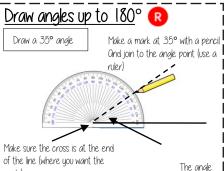
Clockwise: moving in the direction of the hands on a clock

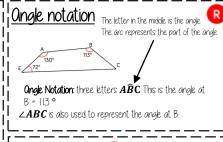
Construct: to draw accurately using a compass, protractor and or ruler or straight edge.

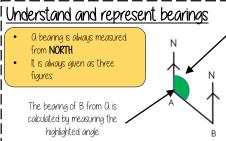
Scale: the ratio of the length of a drawing to the length of the real thing.

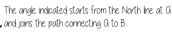
Protractor: an instrument used in measuring or drawing angles.











This angle shows the bearing of **B from** A

The sentence... "Bearing of \_\_\_\_\_ from \_\_\_\_ " is really important in identifying the bearing being represented



Remember: Scale drawings ONLY change lengths and distances. Ongles remain the same

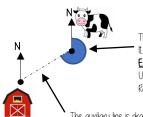






Using estimation it is clear this angle is between 090° and 180°

#### Measure and read bearings



#### The bearing of the cow to the barn

This angle is measured from **NORTH** It is measured in a clockwise direction

Estimation indicates this angle is between 180° and 270° Use a protractor to measure accurately Remember: bearings are written as three figures

The auxiliary line is drawn to help you measure and draw the angle that is measured to represent the bearing

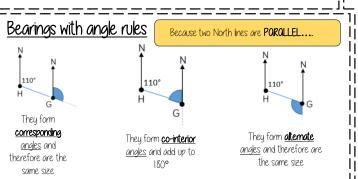
# Scale drawings using bearings Remember change size The bearing measurements do not change from "re to images

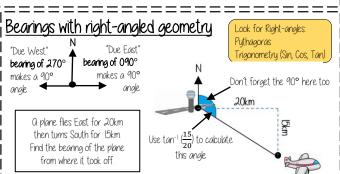
Remember — angles **DO NOT** change size in scaled drawings

The bearing measurements do not change from "real life" to images The units in the ratio scale are the same

The scale may need to be calculated from the image.

| Gcm = 30km | G:3,000,000 | G:3,





## YFAR 10 - GFOMETRY

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## Working with circles

#### What do I need to be able to do?

#### By the end of this unit you should be able to:

- Recognise and label parts of a circle
- Calculate fractional parts of a circle
- Calculate the length of an arc
- Calculate the area of a sector
- Understand and use volume of a cone. culinder and sphere.
- Understand and use surface area of a cone, culinder and sphere.

#### Keywords

Circumference: the length around the outside of the circle — the perimeter

Orea: the size of the 2D surface Diameter: the distance from one side of a circle to another through the centre

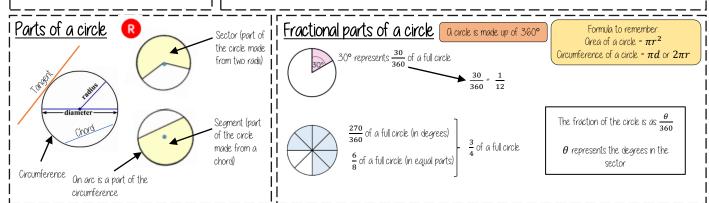
Radius: the distance from the centre to the circumference of the circle

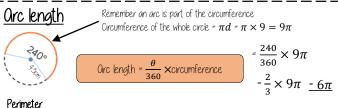
Tangent: a straight line that touches the circumference of a circle

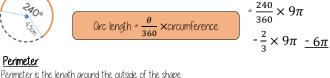
Chord: a line seament connecting two points on the curve Frustrum: a pyramid or cone with the top cut off

Hemisphere: half a sphere

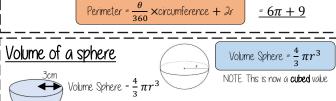
Surface area: the total area of the surface of a 3D shape



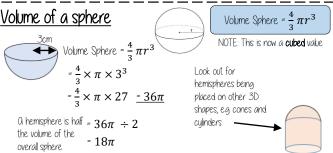


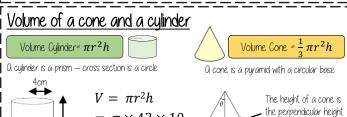


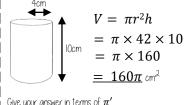
#### Remember a sector is part of a circle • Orea of the whole circle = $\pi r^2 = \pi \times 6^2 = 36\pi$ Sector area $=\frac{120}{360}\times36\pi$ $\frac{\theta}{}$ × area of circle $=\frac{1}{2}\times 36\pi = 12\pi$



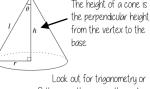
This includes the arc length and the radii that encloses the shape



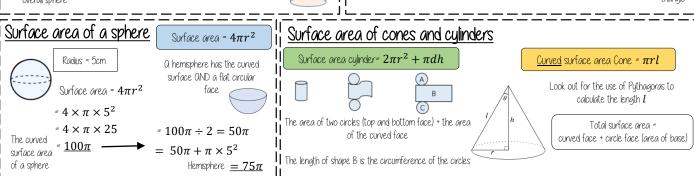




Give your answer in terms of  $\pi'$ 502.7cm<sup>2</sup> means **NOT** in terms of pi



Pythagoras theorem — the radius forms the base of a right-angled trianale



## YEAR 10 - GEOMETRY...

#### @whisto maths

### Vectors

#### What do I need to be able to do?

By the end of this unit you should be able to:

- Understand and represent vectors
- Use and read vector notation
- Draw and understand vectors multiplied by a scalar
- Draw and understand addition of vectors
- Draw and understand addition and subtraction of vectors

#### Keywords

**Direction**: the line our course something is going

Magnitude: the magnitude of a vector is its length

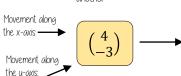
Scalar: a single number used to represent the multiplier when working with vectors

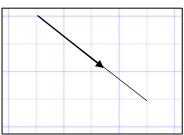
Column vector: a matrix of one column describing the movement from a point

**Resultant**: the vector that is the sum of two or more other vectors **Parallel**: straight lines that never meet

#### Understand and represent vectors

Column vectors have been seen in translations to describe the movement of one image onto another





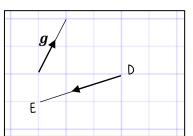
Vectors show both direction and magnitude

The arrow is pointing in the direction from starting point to end point of the vector.

The direction is important to correctly write the vector

The magnitude is the length of the vector (This is calculated using Pythagoras theorem and forming a right-angled triangle with auxiliary lines) The magnitude stays the same even if the direction changes

#### <u>Understand and represent vectors</u>



Vector notation  $\overrightarrow{DE}$  is another way to represent the vector joining the point D to the point E

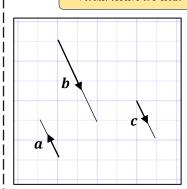
$$\overrightarrow{DE} = \begin{pmatrix} -3 \\ -1 \end{pmatrix}$$

The arrow also indicates the direction from point D to point E

Vectors can also be written in bold lower  $g = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$ 

#### Vectors multiplied by a scalar

Parallel vectors are scalar multiples of each other



 $b = 2 \times c = 2c$ 

Multiply  $m{c}$  by 2 this becomes  $m{b}$ . The two lines are parallel

$$a = -1 \times c = -c$$

The vectors  $m{a}$  and  $m{c}$  are also parallel 0 negative scalar causes the vector to reverse direction

$$a = \begin{pmatrix} -1 \\ 2 \end{pmatrix} b = \begin{pmatrix} 2 \\ -4 \end{pmatrix} c = \begin{pmatrix} 1 \\ -2 \end{pmatrix}$$

 $b = -2 \times a = -2a$ 

#### <u>**Oddition of vectors**</u>

$$\overrightarrow{AB} = \begin{pmatrix} 3 \\ 1 \end{pmatrix}$$

$$\overrightarrow{BC} = \begin{pmatrix} 2 \\ -4 \end{pmatrix}$$

$$= \binom{3}{1} + \binom{2}{-4}$$

$$= \binom{3+2}{1+-4}$$

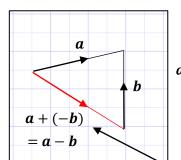
$$\overrightarrow{AC} = \binom{5}{-3}$$

Look how this addition compares to the vector  $\overrightarrow{AC}$ 

 $\overrightarrow{AB} + \overrightarrow{BC}$ 

The resultant  $\overrightarrow{AB} + \overrightarrow{BC} = \overrightarrow{AC} = \begin{pmatrix} 5 \\ -3 \end{pmatrix}$ 

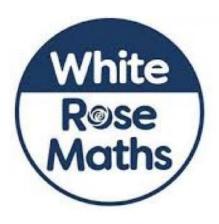
#### Oddition and subtraction of vectors



 $a = \begin{pmatrix} 5 \\ 1 \end{pmatrix}$   $b = \begin{pmatrix} 0 \\ 4 \end{pmatrix}$ 

 $\boldsymbol{a} + (-\boldsymbol{b}) = \begin{pmatrix} 5 + -0 \\ 1 + -4 \end{pmatrix} = \begin{pmatrix} 5 \\ -4 \end{pmatrix}$ 

The resultant is  $m{a} - m{b}$  because the vector is in the opposite direction to b which needs a scalar of -1



BLOCK: PROPORTIONS AND PROPORTIONAL CHANGE

Ratios and fractions
Percentages and Interest
Probability

## YEAR 10 - PROPORTION...

#### @whisto maths

### Ratios and fractions

#### What do I need to be able to do?

#### By the end of this unit you should be able to:

- Compare quantities using ratio
- Link ratios and fractions and make comparisons
- Share in a given ratio
- Link Ratio and scales and graphs
- Solve problems with currency conversions
- Solve 'best buy' problems
- Combine ratios

#### Keywords

Ratio: a statement of how two numbers compare

Equivalent: of equal value

**Proportion**: a statement that links two ratios

Integer: whole number, can be positive, negative or zero.

Fraction: represents how many parts of a whole.

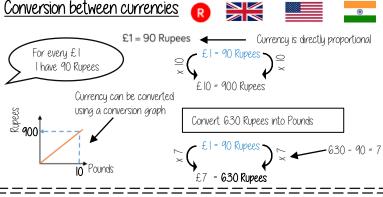
Denominator: the number below the line on a fraction. The number represent the total number of parts.

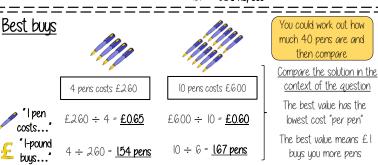
**Numerator**: the number above the line on a fraction. The top number. Represents how many parts are taken

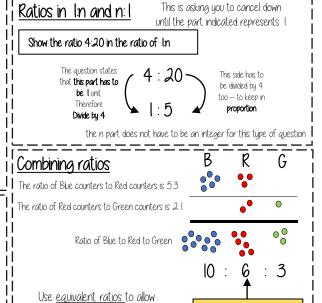
Origin: (0,0) on a graph. The point the two axes cross

Gradient: The steepness of a line

#### Sharing a whole into a given Ratios and fraction Compare with ratio \, 🕟 "For every dog there are 2 cats" Trees ratio James and Lucy share £350 in the Trees: Flowers ratio 3:4 Dogs: Cats A Work out how much each person earns Units have the be of Model the Question James the same Flowers The ratio has to be written in the James: Lucy Fraction of trees value to same order as the information is 3:4 compare given Number of parts of in group ratios e.g. 2:1 would represent 2 dogs for Total number of parts Lucu everu I cat Find the value of one part £350 + 7 = £50 \n/hok: £.350 Ratio and graphs 🔃 Ratio and scale 7 parts to share between = one part (3 James, 4 Lucu) £50 Graphs with a constant ratio are a picture of a car is drawn with a scale of 1:30 Put back into the question directly proportional James = 3 x £50 = £ 150 Form a straight line П James: Lucu Pass through (0,0) The car image is Ш x50 3:4 x50 10cm Image: Real life ▲ £ 150:£200 lcm: 30cm The gradient is the constant ratio 10cm: 300cm **4** Lucy = $4 \times £50 = £200$







comparison of the group that is

common to both statements

Lowest common multiple of

the ratio both statements

## YFAR 10 - PROPORTION

@whisto maths

## Percentages and Interest

#### What do I need to be able to do?

#### Bu the end of this unit you should be able to:

- Convert and compare FDP
- Work out percentages of amounts
- Increase/ decrease by a given percentage
- Express one number as a percentage
- Calculate simple and compound interest
- Calculate repeated percentage change
- Find the original value
- Solve problems with growth and decay

#### Keywords

**Exponent**: how many times we use a number in multiplication. It is written as a power Compound interest: calculating interest on both the amount plus previous interest

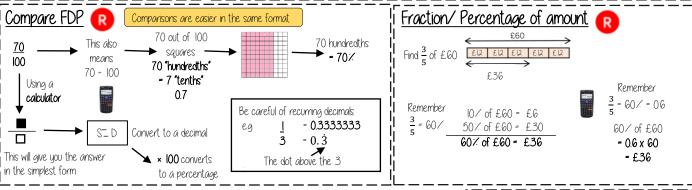
**Depreciation**: a decrease in the value of something over time.

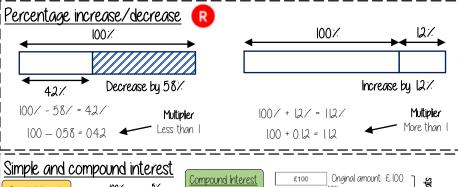
Growth: where a value increases in proportion to its current value such as doubling.

**Decay:** the process of reducing an amount by a consistent percentage rate over time.

Multiplier: the number you are multiplying by

Equivalent: of equal value.





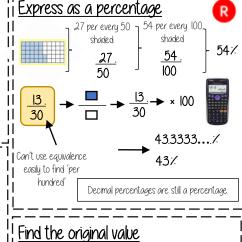
Tess invests

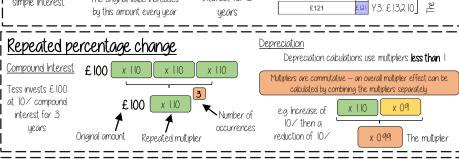
£100 at 10%

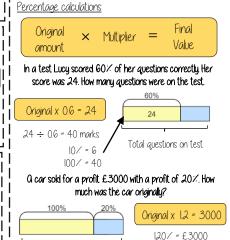
compound

interest for 3

The original value increases



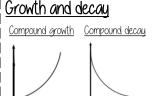




£3000

10% = £250

100% = £2500



Simple Interest

James invests

£2000 at 5%

simple interest

Compound growth and compound decay are exponential graphs

Decay — the values get closer to 0 The constant multiplier is less than one

<u>Growth</u> — the values increase exponentially The constant multiplier is more than one

Y1: £110

Y2: £121

£10

£100

## YFAR 10 - PROPORTION...

#### @whisto\_maths

## Probability

#### What do I need to be able to do?

#### By the end of this unit you should be able to:

- Odd, Subtract and multiply fractions
- Find probabilities using likely outcomes
- Use probability that sums to 1
- Estimate probabilities
- Use Venn diagrams and frequency trees
- Use sample space diagrams
- Calculate probability for independent events
- Use tree diagrams

Oddition and Subtraction

#### Keywords

**Event**: one or more outcomes from an experiment

Outcome: the result of an experiment.

Intersection: elements (parts) that are common to both sets

Union: the combination of elements in two sets.

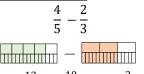
Expected Value: the value / outcome that a prediction would suggest you will get

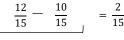
Universal Set: the set that has all the elements

Systematic: ordering values or outcomes with a strategy and sequence

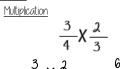
**Product**: the answer when two or more values are multiplied together.

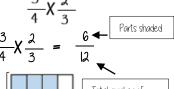
#### Odd, Subtract and multiply fractions



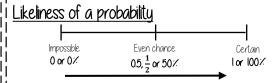


Use equivalent fractions to find a common multiple for both denominators





Total number of parts in the diagram



The more likely an event the further up the probability it will be in comparison to another event. (It will have a probability closer to 1) --------



Probability is always a value between 0 and 1

The probability of getting a blue ball is  $\frac{1}{2}$ :The probability of **NOT** getting a blue ball is  $\frac{4}{5}$ 

26)

The sum of the probabilities is

60

#### Experimental data

Theoretical probability

What we expect to happen

Experimental

What actually happens when we probabilitu try it out

completed the closer experimental probability and theoretical probability become

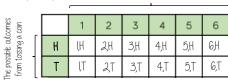
The more trials that are

The probability becomes more accurate with more trials. Theoretical probability is proportional

==========

Modelled:

#### **Sample space** The possible outcomes from rolling a dice



P (Even number and tales)

#### Tables, Venn diagrams, Frequency trees

Frequency trees 60 people visited the zoo one Saturday mornin 26 of them were adults. 13 of the adult's

favourite animal was an elephant. 24 of the children's favourite animal was an elephant.

#### Two-way table

|          | Odult | Child | Total |
|----------|-------|-------|-------|
| Elephant | 13    | 24    | 37    |
| Other    | 13    | 10    | 23    |
| Total    | 26    | 34    | 60    |

way tables can show the same information

The total columns on twoway tables show the possible denominators

Frequency trees and two-

 $P(adult) = \frac{26}{10}$ 

P(Child with favourite animal as elephant) = 13

#### Venn diagram



in set A QND set B $P(A \cap B)$ 

in set A OR set B

 $P(A \cup B)$ 

P(A)

in set ANOT in set A

#### Independent events

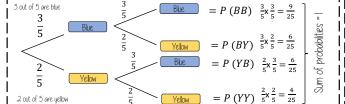
The outcome of two events happening. The outcome of the first event has no bearing on the outcome of the other

P(A and B)

 $= P(A) \times P(B)$ 

#### Tree diagram for independent event

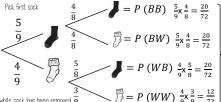
lsobel has a bag with 3 blue counters and 2 yellow. She picks a counter and replaces it before the second pick Because they are replaced the second pick has the same probability



#### Dependent events Tree diagram for dependent

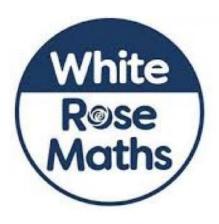
The outcome of the first event has an impact on the second event

O sock drawer has 5 black and 4 white socks, Jamie picks 2 socks from the drawer



NOTE: as "socks" are removed from the drawer the number of items in that drawer is also reduced .. the denominator is also reduced for the second pick.

P(A')



BLOCK: DELVING INTO DATA

Collecting, representing and interpreting data

## 10 — DELVING INTO DATA

@whisto maths

## Collecting, representing and interpreting

#### What do I need to be able to do?

#### Bu the end of this unit you should be able to:

- Construct and interpret frequency tables and polygon. two-way tables, line, bar, & pie 1
- Find and interpret averages from a list and
- Construct and interpret time series graphs, stem and leaf diagrams and scatter araphs

#### Keywords

Population: the whole group that is being studied

Sample: a selection taken from the population that will let you find out information about the larger group Representative: a sample group that accurately represents the population

Random sample: a group completely chosen by change. No predictability to who it will include.

Bias: a built-in error that makes all values wrong by a certain amount

Primary data: data collected from an original source for a purpose.

Secondary data: data taken from an external location. Not collected directly.

Outlier: a value that stands apart from the data set

#### Frequency tables and polygons

| x<br>Weight(g)  | Frequency |
|-----------------|-----------|
| $40 < x \le 50$ | 1         |
| $50 < x \le 60$ | 3         |
| $60 < x \le 70$ | 5         |

We do not know from grouped data where each value is placed so have to use an estimate for calculations

MID POINTS Mid-points are used as estimated values for grouped data. The middle of each group

Each point is plotted at them mid point for the group it represents Each point is connected with a straight line. Weight (g)

The data about weiaht starts at 40. So the axis can start at 40

Mid-point Start point + End point

#### Two way tables

60 people visited the zoo one Saturday morning 26 of them were adults 13 of the adult's favourite animal was an elephant. 24 of the children's favourite animal was an elephant

> Extract information to input to the two-way table

Subgroups each have their own heading

|          | Odult | Child | Total |  |
|----------|-------|-------|-------|--|
| Elephant | 13    | 24    | 37    |  |
| Other    | 13    | 10    | 23    |  |
| Total    | 26    | 34    | 60 🗸  |  |
|          |       |       |       |  |

Needs subgroup totals

Overall total

Compare the bars green compared to yellow. The Bar and line charts size of each bar is the frequency Composite bar charts Overall total easily comparable Dual bar charts

side. Categories clearly indicated

Bars are compared side by Easier to compare subgroups Categories clearly indicated

Draw and interpret Pie Charts There were 60 people asked in this survey (Total frequency)

This is 192°

"32 out of 60 people had a dog"

This fraction of the 360 degrees represents dogs <u>32</u> x 360 = 192°

Os 60 goes into 360 — 6 times. Each frequency can be multiplied by 6 to find the degrees (proportion of 360)

Comparing Pie Charts: You NEED the overall Use a protractor to draw frequency to make any comparisons

#### Overages from a table

Overall Frequency: Non-grouped data 20 Number of Siblings () 6 Frequencu 0 12 Subtotal Total number of siblings: 20

The data in a list: 0,0,0,0,0,0,1,1,1,1,1,1,1,2,2,2,2,2

Mean: total number of siblings Total frequency

#### Grouped data

| X<br>W::+v(-)             | Frequency | Mid Point | MP x Freq |
|---------------------------|-----------|-----------|-----------|
| Weight(g) $40 < x \le 50$ | 1         | 45        | 45        |
| 50 < <i>x</i> ≤ 60        | 3         | 65        | 195       |
| 60 < <i>x</i> ≤ 70        | 5         | 65        | 325       |

Overall Frequency: 9 Overall Total: 565

Mean: 628g

#### Overages from lists

The Mean

a measure of average to find the central tendency... a typical value that represents the data

24, 8, 4, II, 8,

Find the sum of the data (add the values

55 Divide the overall total by how many pieces of data you have

 $55 \div 5$ 

Mean = 11

#### The Mode (The modal value)

This is the number OR the item that occurs the most (it does not have to be numerical)

24, 8, 4, 11, 8,

This can still be easier if it the data is ordered first

Mode = 8

The Median

The value in the center (in the middle) of the data

24, 8, 4, II, 8

Put the data in order

4, 8, 8, 11, 24

Find the value in the middle 4, 8, 8, 11, 24

Median = 8

NOTE: If there is no single middle value find the mean of the two numbers left

#### For Grouped Data

The modal group — which group has the highest frequency,

The data in a list: 45, 55, 55, 55, 65, 65, 65, 65, 65

## 10 — DELVING INTO DATA

@whisto maths

## Collecting, representing and interpreting

#### What do I need to be able to do?

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#### Stem and leaf

O way to represent data and use to find averages

This stem and leaf diagram shows the age of people in a line at the supermarket.

0 | 7 9 4 5 6 8 8 Key: 1 4 Means 14 years old

1 3 2

Stem and leaf diagrams:

Must include a key to explain what it represents The information in the diagram should be ordered

#### Back to back stem and leaf diagrams

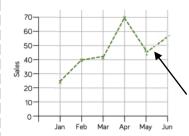
| Girls                                                             |    | Boys                   |                   |
|-------------------------------------------------------------------|----|------------------------|-------------------|
| 5                                                                 | 14 |                        |                   |
| 7, 5, 5, 5, 4<br>8, 4, 2, 1, 0<br>9, 8, 7, 6, 6, 4, 2, 1, 1, 0, 0 | 15 | 3, 8, 9                | 15 3,             |
| 8, 4, 2, 1, 0                                                     | 16 | 2, 5, 7, 7, 7, 8, 8, 9 | Means 153 cm tall |
| 9, 8, 7, 6, 6, 4, 2, 1, 1, 0, 0                                   | 17 | 0, 2, 3, 6, 6, 7, 7    |                   |
|                                                                   | 18 | 0, 1, 4, 5             |                   |

Back to back stem and leaf diagrams Ollow comparisons of similar groups

Ollow representations of two sets of data

#### Time-Series

This time-series graph shows the total number of car sales in £ 1000 over time



Look for general trends in the data. Some data shows a clear increase or a clear decrease over time

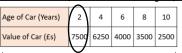
Readings in-between points are estimates (on the dotted lines). You can use them to make assumptions.

#### Comparing distributions

Comparisons should include a statement of average and central tendency, as well as a statement about spread and consistency

Mean, mode, median — allows for a comparison about more or less average Range — allows for a comparison about reliability and consistency of data

#### Draw and interpret a scatter graph.



- This data may not be given in size order
- The data forms information pairs for the scatter graph
- Not all data has a relationship

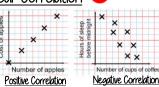
The link between the data can be explained verbally

This scatter graph show as the age of a car increases the value decreases

8000-(Es)

The axis should fit all the values on and be equally spread out

#### Linear Correlation



Os one variable increases the

No Correlation There is no

Os one variable increases so does the other other variable variable decreases

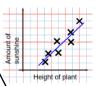
relationship between the two variables

#### The line of best fit

The Line of best fit is used to make estimates about the information in your scatter graph

#### Things to know

- The line of best fit <u>DOES NOT</u> need to go through the origin (The point the axes cross)
- There should be approximately the same number of points above and below the line (It may not go through any points)
- The line extends across the whole



is only an estimate because the line is designed to be an average representation of the data

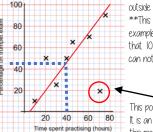
It is always a straight line.

#### Using a line of best fit

**Interpolation** is using the line of best fit to estimate values inside our data

e.g. 40 hours revising predicts a percentage of 45.

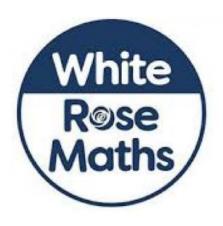
## 100



Extrapolation is where we use our line of best fit to predict information outside of our data \*\*This is not always useful — in this

example you cannot score more that 100%. So revising for longer can not be estimated \*\*

This point is an "outlier" It is an outlier because it doesn't fit this model and stands apart from



BLOCK: USING NUMBER

Non-calculator methods

Types of number and sequences

Indices and Roots

## YFAR 10 - USING NUMBER

#### @whisto maths

### Non-calculator methods

#### What do I need to be able to do?

Bu the end of this unit you should be able to:

- Use mental/written methods for the four number operations
- Use four operations for fractions
- Write exact answers
- Round to decimal places and significant figures
- Estimate solutions
- Understand limits of accuracy
- Understand financial maths

#### Keuwords

Truncate: to shorten, to shorten a number (no rounding), to shorten a shape (remove a part of the shape)

Round: making a number simpler, but keeping its place value close the what it originally was

Credit: money that goes into a bank account

Debit: money that leaves a bank account

**Profit**: the amount of money after income - costs

Tax: money that the government collects based on income, sales and other activities.

Balance: The amount of money in a bank account

Overestimate: Rounding up — gives a solution higher than the actual value

Underestimate: Rounding down — gives a solution lower than the actual value

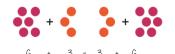
#### Oddition/Subtraction



Modelling methods for addition/subtraction

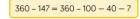
- Bar models
- Number lines
- Part/ Whole diagrams

Oddition is commutative



The order of addition does not change the result

Subtraction the order has to stay the same

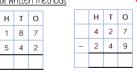


- Number lines help for addition and subtraction
- Working in 10's first aids mental addition/subtraction
- Show your relationships by writing fact families

Multiplication methods

Formal written methods

1



Remember the place value of each column. You may need to move 10 ones to the ones column to be able to subtract

#### Decimals have the same methods remember to align the place value

#### Division methods

Division with decimals

3584 ÷ 7 = 512

S<u>hort division</u> <sup>3</sup>5

 $\div 24 = \div 6 \div 4$ Break up the divisor using factors

The placeholder in division methods is essential — the decimal lines up on the dividend and the quotient

All give the same solution as represent the same proportion. Multiply the values in proportion until the divisor becomes an integer

→ 24 ÷ 02 -

Long <u>multiplication</u> (column)

Grid method

Less effective method especially for bigger multiplication

#### Multiplication with decimals

Perform multiplications as integers 

Make adjustments to your answer to match the question:  $0.2 \times 10 = 2$  $0.3 \times 10 = 3$ 

Therefore 6 ÷ 100 = 0.06

#### Four operations with fractions

Od<u>dition and Subtraction</u>



#### Multiplication



5

addition

Multiplying by a reciprocal gives the

outcome



#### Exact Values



 $=\frac{1}{2}\times 36\pi = 12\pi$ 

Leave as a surd

Tan 30 =  $\frac{1}{\sqrt{3}}$ 

#### Estimation 🔃

Round to I significant figure to estimate

 $21.4 \times 3.1 \approx 20 \times 3 \approx 60$ 

The equal sign changes to show it is an estimation

This is an **underestimate** because both values were rounded down

It is good to check all calculations with an estimate in all aspects of maths — it helps you identify calculation errors.

#### Limits of accuracu

O width  $oldsymbol{w}$  has been rounded to 6.4cm correct to dp

< 6.35 the values > 6.45 the values wou Error interval would round to 6.3

The error interval

 $6.35 \le w < 6.45$ 

Only value within these limits would round to 6.4 to 1dp

O width  $\boldsymbol{w}$  has been truncated to 6.4cm correct to 1dp. Error interval < 6.4 the values would truncate to 6.3 > 6.5 the values would

 $6.4 \le w < 6.5$ 

Ony value within these limits would truncate to 6.4 to 1dp

### Rounding 🔃

2.46 192 (to 12dp) - Is this closer to 246 or 247

2.46

247

This shows the number is closer

2.46 192

Significant Figures

370 to 1 significant figure is 400 37 to 1 significant figure is 40 3.7 to I significant figure is 4

0.37 to I significant figure is 0.4 0.00000037 to 1 significant figure is 0.0000004 SF: Round to the first nonzero number

## YEAR 10 - USING NUMBER..

#### @whisto maths

## Types of number & sequences

#### What do I need to be able to do?

#### By the end of this unit you should be able to:

- Understand factors and multiples
- Express numbers as a product of primes
- Find the HCF and LCM
- Describe and continue sequences
- Explore sequences
- Find the nth term of a linear sequence

#### Keywords

Factor: numbers we multiply together to make another number

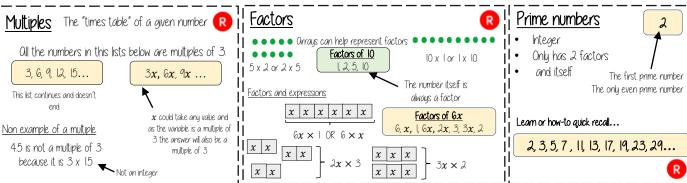
Multiple: the result of multiplying a number by an integer.

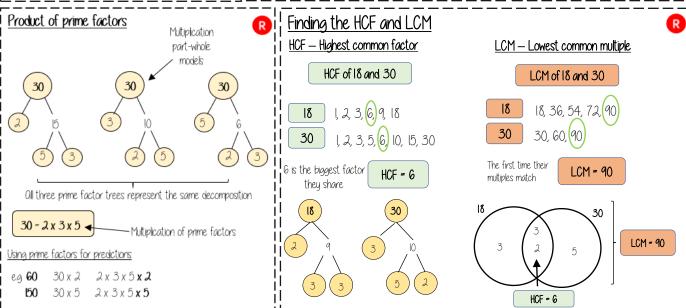
HCF: highest common factor. The biggest factor that numbers share.

LCM: lowest common multiple. The first multiple numbers share.

**Orithmetic:** a sequence where the difference between the terms is constant

**Geometric**: a sequence where each term is found by multiplying the previous one by a fixed nonzero number **Sequence**: items or numbers put in a pre-decided order





#### <u> Orithmetic/Geometric sequences</u>

Orithmetic Sequences change by a common difference. This is found by addition or subtraction between terms

**Geometric Sequences** change by a common ratio. This is found my multiplication/division between terms.

**Term to term rule** — how you get from one term (number in the sequence) to the next term.

**Position to term rule** — take the rule and substitute in a position to find a term Eg. Multiply the position number by 3 and then add 2

#### 11 Other sequences

Fibonacci Sequence 1, 1, 2, 3, 5, 8 ...

II Triangular Numbers — look at the formation

Each term is the

sum of the previous

l, 3, 6, 10, 15 ...

📙 Square Numbers — look at the formation



Sequences are the repetition of a patten

#### i Finding the nth term

This is the 4  $\longrightarrow$  4, 8, 12, 16, 20....

4n

This has the same constant difference — but is 3 more 7, 11, 15, 19, 22

than the original sequence -4n + 3 =

This is the constant difference between the terms in the sequence This is the comparison (difference) between the original and new sequence

## YFAR 10 - USING NUMBER

#### @whisto maths

### Indices & Roots

#### What do I need to be able to do?

#### By the end of this unit you should be able to:

- Identify square and cube numbers
- Calculate higher powers and roots
- Understand powers of 10 and standard
- Know the addition and subtraction rule for
- Understand power zero and negative indices

#### Keywords

Standard (index) Form: A system of writing very big or very small numbers

**Commutative:** an operation is commutative if changing the order does not change the result.

Base: The number that gets multiplied by a power

**Power**: The exponent — or the number that tells you how many times to use the number in multiplication. Exponent: The power — or the number that tells you how many times to use the number in multiplication.

**Indices**: The power or the exponent.

Negative: a value below zero...

Coefficient: The number used to multiply a variable

#### Calculate with numbers in standard form $lackbr{R}_{11}^{11}$ Higher powers and roots Cube numbers Square and cube numbers 144 Square numbers (number of times | 📒 l. 4, 9 , l6... 1, 8, 27, 64, 125... multiplied by 1 itself) | the base 144 = 2x2x2x2x3x3 **216 =** 2 x 2 x 2 x 3 x 3 x 3 number 2x2x3x2x2x3[2x3]x[2x3]x[2x3] Finding the nth Prime factors can find square root root of any value $\sqrt[3]{216} = 6$ $\sqrt{144} = 12$ Other mental strategies for square roots Standard form $\sqrt{810000} = \sqrt{81} \times \sqrt{10000}$ Ony integer 0.001 100 1000 $= 9 \times 100$ Onu number $|\chi|_{\frac{1}{1000}}$ 10-2 10-3 = 900less than 10 1 x 10-3 Negative powers do not Oddition/Subtraction Laws Ony value to the power O always = 1 Example Non-example indicate negative solutions 3.2 x 10 4 0.8 x 10 4 Numbers in standard form with negative

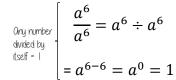
#### Zero and negative indices

5.3 x 10<sup>07</sup>

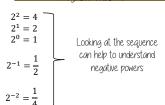
= 3.2 x 10 x 10 x 10 x 10

= 32000

$$x^0 = 1$$



#### Negative indices do not indicate negative solutions



#### Powers of powers

$$(x^a)^b = x^{ab}$$

powers will be less than I

 $3.2 \times 10^{-4} = 3.2 \times \frac{1}{10} \times \frac{1}{10} \times \frac{1}{10} \times \frac{1}{10} = 000032$ 

$$(2^3)^4 = 2^3 \times 2^3 \times 2^3 \times 2^3$$

The same base and power is repeated Use the addition

$$(2^3)^4 = 2^{12} - a \times b = 3 \times 4 = 12$$

NOTICE the difference

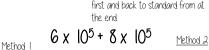
$$(2x^3)^4 = 2x^3 \times 2x^3 \times 2x^3 \times 2x^3$$

The addition law applies ONLY to the powers. The integers still need to be multiplied

 $(2x^3)^4 = 16x^{12}$ 

#### Standard form calculations

Oddition and Subtraction Tip: Convert into ordinary numbers first and back to standard from at



= 600000 + 800000

= 1400000

 $= 1.4 \times 10^{5}$ 

14 x 10<sup>5</sup> This is not the 1.4 x 101 x 105

 $= (6 + 8) \times 10^{5}$ 

 $a^m \times a^n = a^{m+n}$ 

 $a^m \div a^n = a^{m-n}$ 

final answer = 1.4 x 10<sup>5</sup> Multiplication and division



((1.5**)**x 10<sup>5</sup>) ÷ (0.3**)**x 10<sup>3</sup>)

 $1.5 \div 0.3$  x  $10^5 \div 10^3$ 

 $=5 \times 10^{2}$ 

For multiplication and division you can look at the values for A and the powers of 10 as two separate calculations